

Free Fall II



$$v_1 = 6.0 \text{ m/s}$$

$$\Delta d = 2.0 \text{ m}$$

$$a = -9.8 \text{ m/s}^2$$

$$\Delta t = ?$$

$$1^{st} \quad \sqrt{v_f^2 = v_i^2 + 2a\Delta d}$$

$$v_f = \sqrt{(6.0 \text{ m/s})^2 + 2(-9.8 \text{ m/s}^2)(-2.0 \text{ m})}$$

$$v_f = \sqrt{36 \text{ m}^2/\text{s}^2 + 39.2 \text{ m}^2/\text{s}^2} = \sqrt{75.2 \text{ m}^2/\text{s}^2}$$

$$v_f = \pm 8.67 \text{ m/s} = \boxed{-8.67 \text{ m/s}}$$

$$2^{nd} \quad \Delta d = \frac{v_i + v_f}{2} \Delta t$$

$$\Rightarrow \Delta t = \frac{2\Delta d}{v_i + v_f} = \frac{2(-2 \text{ m})}{(6.0 \text{ m/s} + -8.67 \text{ m/s})} = \frac{-4 \text{ m}}{-2.67 \text{ m/s}} = \boxed{1.55}$$



$$v_i = 0$$

$$\Delta d = -24,000 \text{ m}$$

$$a = -3.7 \text{ m/s}^2$$

$$\Delta t = ?$$

$$v_f = ?$$

$$\text{For } \Delta t: \Delta d = v_i \Delta t + \frac{1}{2} a \Delta t^2$$

$$\Delta t = \sqrt{\frac{2\Delta d}{a}} = \sqrt{\frac{-48,000 \text{ m}}{-3.7 \text{ m/s}^2}} = \sqrt{12,973 \text{ s}^2}$$

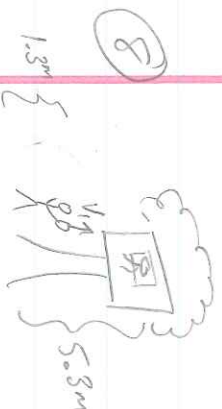
$$\Delta t = 114 \text{ s}$$

$$= \boxed{1 \text{ min } 54 \text{ s}}$$

$$\text{For } v_f: v_f^2 = v_i^2 + 2a\Delta d$$

$$v_f = \sqrt{2(-3.7 \text{ m/s}^2)(-24,000 \text{ m})} = \sqrt{177,600 \text{ m}^2/\text{s}^2}$$

$$v_f = \pm 421 \text{ m/s} = \boxed{-421 \text{ m/s}}$$



$$v_i = 2.4 \text{ m/s}$$

$$\Delta d = 1.3 \text{ m}$$

$$a = -9.8 \text{ m/s}^2$$

$$a) \text{ } d_f \geq 5.3 \text{ m}?$$

$$\Delta d = d_f - d_i \Rightarrow d_f = \Delta d + d_i$$

$$\text{@ peak } v_f = 0, \text{ so}$$

$$v_f = v_i + a\Delta d \Rightarrow \Delta d = \frac{-v_f}{2a} = \frac{-(2.04 \text{ m/s})}{2(-9.8 \text{ m/s}^2)}$$

$$\Delta d = 0.12 \text{ m} \text{ so } d_f = 2.05 \neq 5.3 \text{ No}$$

$$b) \Delta t = ?$$

$$\Delta d = -1.3 \text{ m}$$

$$1^{st} \quad v_f^2 = v_i^2 + 2a\Delta d$$

$$v_f = \sqrt{(2.4 \text{ m/s})^2 + 2(-9.8 \text{ m/s}^2)(-1.3 \text{ m})}$$

$$v_f = \sqrt{11.64 \text{ m}^2/\text{s}^2} = (3.4 \text{ m/s})$$

$$2^{nd}$$

$$\Delta d = \frac{v_i + v_f}{2} \Delta t \Rightarrow \Delta t = \frac{2\Delta d}{v_i + v_f} = \frac{2(-1.3 \text{ m})}{2.4 \text{ m/s} + -3.4 \text{ m/s}} = \frac{-2.6 \text{ m}}{-1 \text{ m/s}}$$

$$\Delta t = 2.6 \text{ s}$$

Free Fall II

9. For accelerations are the same

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I
 $a_1 = 29.4 \text{ m/s}^2$
 $(v_{1i} = 0)$
 $\Delta t_1 = 4.00 \text{ s}$

II
 $v_{12} = v_{11}$
 $a_2 = -9.8 \text{ m/s}^2$
 $(v_f = 0)$
 v_{a2}

① $\Delta d = \Delta d_1 + \Delta d_2$

$\Delta d_1 = v_{1i} \Delta t_1 + \frac{1}{2} a_1 \Delta t_1^2$

$\Delta d_1 = \frac{1}{2} (29.4 \text{ m/s}^2) (4.00 \text{ s})^2$

$(\Delta d_1 = 235.2 \text{ m})$

② $v_{f1} = v_{1i} + a_1 \Delta t$

$= (29.4 \text{ m/s}) (4 \text{ s})$

$(= 117.6 \text{ m/s})$

③ $v_{f2} = 0$

$v_{f2}^2 = v_{12}^2 + 2 a_2 \Delta d_2$

$\Rightarrow \Delta d_2 = \frac{-v_{12}^2}{2a_2} = \frac{-(117.6 \text{ m/s})^2}{2(-9.8 \text{ m/s}^2)} = \frac{-13830 \text{ m}^2/\text{s}^2}{-19.6 \text{ m/s}^2}$

$(\Delta d_2 = 705 \text{ m})$

$\Delta d = 235.2 \text{ m} + 705 \text{ m} = \boxed{940 \text{ m}}$



$v_{1A} = 14.7 \text{ m/s}$

$v_{1B} = -14.7 \text{ m/s}$

$a = -9.8 \text{ m/s}^2$

$\Delta d = -19.6 \text{ m}$

$v_{fA}^2 = v_{1A}^2 + 2 a \Delta d$

$v_{fA} = \sqrt{(14.7 \text{ m/s})^2 + 2(-9.8 \text{ m/s}^2)(-19.6 \text{ m})}$

$v_{fA} = \sqrt{216.1 \text{ m}^2/\text{s}^2 + 384.2 \text{ m}^2/\text{s}^2}$

$v_{fA} = \pm 24.5 \text{ m/s} = (-24.5 \text{ m/s})$

$(v_{fB} \text{ also } = -24.5 \text{ m/s})$

To find time $\Delta d = \frac{v_f + v_i}{2} \Delta t = \Delta t = \frac{2 \Delta d}{v_i + v_f}$

$\Delta t_A = \frac{2(-19.6 \text{ m})}{-14.7 \text{ m/s} + -24.5 \text{ m/s}} = \frac{-39.2 \text{ m}}{-39.2 \text{ m/s}} = 1 \text{ s}$

$\Delta t_B = \frac{2(-19.6 \text{ m})}{14.7 \text{ m/s} + -24.5 \text{ m/s}} = \frac{-39.2 \text{ m}}{-9.8 \text{ m/s}} = 4 \text{ s}$

① Difference in time is 3 s

B. Velocity of each ball is -24.5 m/s

C. $\Delta d_A = v_i \Delta t + \frac{1}{2} a \Delta t^2 = (-14.7 \text{ m/s})(0.8 \text{ s}) + \frac{1}{2} (-9.8 \text{ m/s}^2)(0.8 \text{ s})^2 = -11.76 \text{ m} - 3.136 \text{ m} = -14.896 \text{ m}$

$\Delta d_2 = v_i \Delta t + \frac{1}{2} a \Delta t = (14.7 \text{ m/s})(0.8 \text{ s}) + \frac{1}{2} (-9.8 \text{ m/s}^2)(0.8 \text{ s})^2 = 11.76 \text{ m} - 3.136 \text{ m} = 8.624 \text{ m}$

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