## Chapter 5

## The Normal Model

Your calculator knows the Normal model. Take a look under $\mathbf{2}^{\text {ND }}$ DIST. There you will see three "norm" functions: normalpdf(, normalcdf, and invNorm(.


- normalpdf( is one you won't use very often - if at all. There's no need to play around with this one.
- invNorm( will be used in just a minute. Hold off on it for now.
normalcdf( is the one we want. It finds the area under the Normal curve between two cut points. By specifying normalcdf( zLeft, zRight ), you will ask the calculator to find the area in question. DO make friends with this function! ©


## When You Know the Two Cut Points



This example shows a Normal model with cut points of $z=-0.5$ and $z=1.0$. We'd like the calculator to tells us the area under the curve. (We know it's 0.533 , just so we can check that we're doing it correctly.)
normalcdf(-5, 1. (6)
normalcdf(-.5,1.


Select 2:normalcdf(, hit ENTER.
Specify the cut points as normalcdf( $-.5, \mathbf{1 . 0}$ ), and hit ENTER again.

There it is... 0.533 . Approximately $53 \%$ of the Normal model lies between half a standard deviation below and one standard deviation above the mean.

## When You Know Only One Cut Point



Here we see that the shaded area under the curve begins at negative infinity and cuts off at 1.80 . How do you tell the calculator that one of your cut points involves infinity?

Recall that for a Normal model almost all of the area is contained within three standard deviations below the mean through three standard deviations above the mean. So any cut point that is further than 3 will do. Using 5 is fine. So is 36 . The text suggests 99 (and -99, when the cut point is negative infinity) because these values are easy to remember and way beyond any meaningful location.

| $8 \mathrm{nrmalng}(-99,1$. |
| ---: |
| .9646697345 |

Use the command normalcdf( $\mathbf{- 9 9}, \mathbf{1 . 8})$. There you are! The Normal model estimates that approximately $96.4 \%$ of the area under the curve is accounted for.

## Working Backwards

If you know the area that's shaded under the Normal curve and you want to find the z-score (the cut point) that's associated with it, use the invNormal( command.


In terms of standard deviations, where does the $25^{\text {th }}$ percentile fall?

Enter invNormal(.25) and press ENTER. The $25^{\text {th }}$ percentile has an approximate z -score of -0.674 .

What z-score cuts off the highest $10 \%$ of a Normal model?
Remember how to specify the percentile, and the question is easily solved. Cutting off the top $10 \%$ of the curve means that you're looking for the z -score located at the $90^{\text {th }}$ percentile mark.

Enter invNormal(.90) and press ENTER.
The z -score in question is about 1.28 standard deviations above the mean.

